



Stable Boundary Layer Wind Profiles

A Comparison of Analytical Models and LiDAR Observations

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EERA DeepWind Conference 2025
Session 1B: Met-ocean conditions

15.01.2025, Trondheim

Atmospheric Stability and Wind Turbine Response

Thermal stratification influences the loading and power production of wind turbines through effects on:

1. Mean wind profiles:

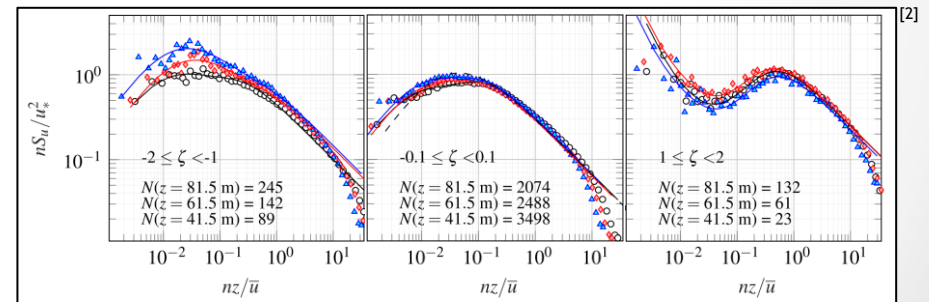
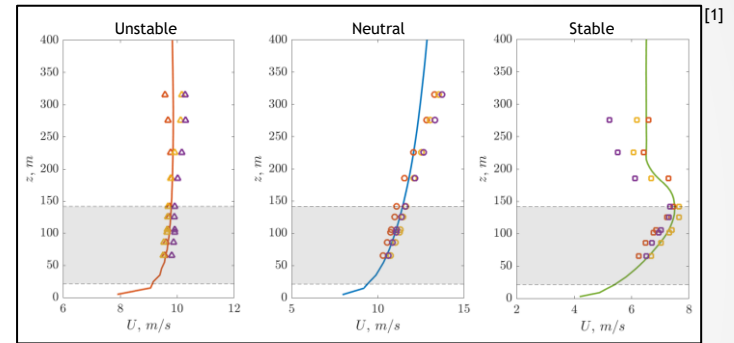
- Wind shear
- Wind veer

2. Turbulence characteristics:

- Turbulence intensity
- Turbulence spectra
- Coherence

3. Wake behaviour:

- Wake recovery
- Wake meandering
- Wake skewing



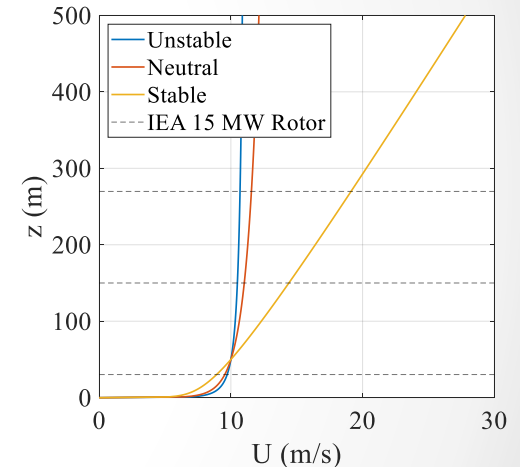
Atmospheric Stability and the Mean Wind Profile

Within the surface layer, effects of thermal stratification are efficiently represented using the logarithmic wind profile:

- $$U(z) = \frac{u_*}{\kappa} \left[\ln \left(\frac{z}{z_0} \right) - \psi \right]$$
- Stability correction: $\psi = f(z, L)$

However, in stable atmosphere, surface layer theory:

- tends to overestimate wind speeds above the surface layer.
- does not account for frequently occurring low-level jets.^[3,4]
- does not account for frequently occurring wind veering.^[1,5]



- [1] Chanprasert, Warit, Sharma, Rajnish N., Cater, John E. and Norris, Stuart E. "Observation and Large Eddy Simulation of Coastal Winds at Anholt Offshore Wind Farm." Journal of Physics: Conference Series. Vol. 2362 No. 1 (2022): p. 012008. DOI 10.1088/1742-6596/2362/1/012008.
- [3] De Jong, Emily, Quon, Eliot and Yellapantula, Shashank. "Mechanisms of Low-Level Jet Formation in the US Mid-Atlantic Offshore." Journal of the Atmospheric Sciences. Vol. 81 No. 1 (2024): pp. 31-52. DOI 10.1175/JAS-D-23-0079.1.
- [4] Borvarán, Dager, Peña, Alfredo and Gandoín, Rémi. "Characterization of offshore vertical wind shear conditions in Southern New England." Wind Energy. Vol. 24 No. 5 (2021): pp. 465-480. DOI 10.1002/we.2583.
- [5] Berg, Jacob, Mann, Jakob and Patton, Edward G. "Lidar-observed stress vectors and veer in the atmospheric boundary layer." Journal of Atmospheric and Oceanic Technology. Vol. 30 No. 9 (2013): pp. 1961-1969. DOI 10.1175/JTECH-D-12-00266.1.

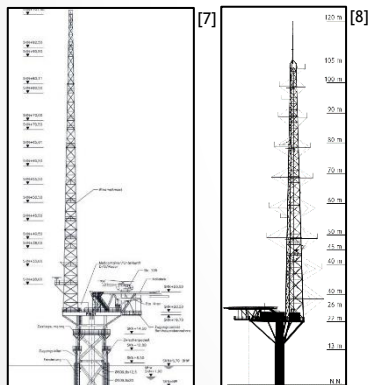
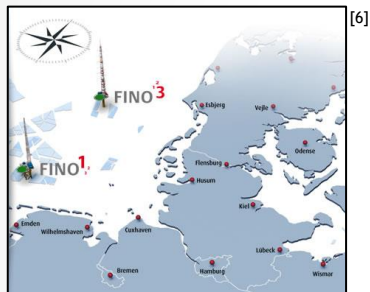
Overview

Stable Boundary Layer Wind Profiles - A Comparison of Analytical Models and LiDAR Observations

- Datasets
- Analytical Wind Profile Models
 - Theory
 - Parametrization
- Wind Profile Comparisons
- Conclusion



Datasets



FINO1

June 2015 -
Oct. 2016

WindCube 100S
 $z = 78 \dots 3528$ m
with $dz = 25$ m

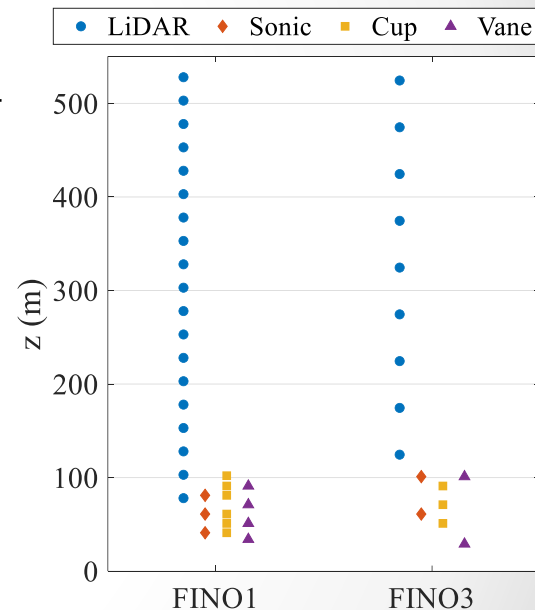
Mast data at
 $z = 34 \dots 102$ m

FINO3

Aug. 2013 -
Oct. 2014

WindCube WLS70
 $z = 125 \dots 2025$ m
with $dz = 50$ m

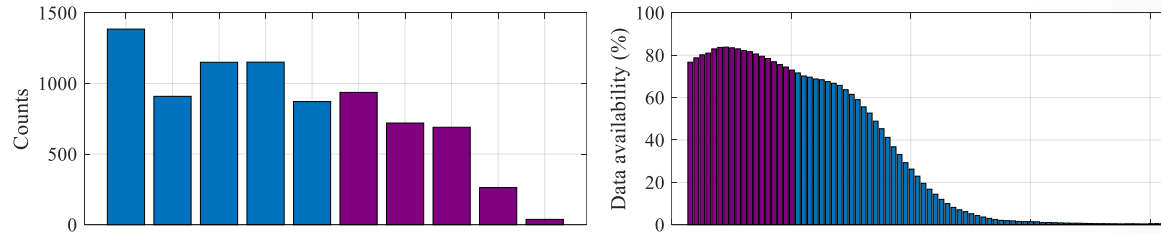
Mast data at
 $z = 29 \dots 101$ m



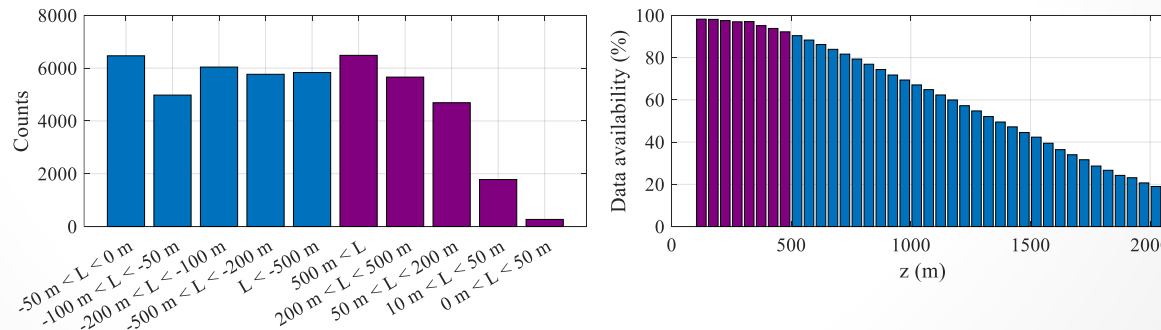
Data Filtering

- 10-min. averaged LiDAR profiles classified using ERA5 Obukhov length estimate.
- Observations filtered for $L \geq 0$ m and $z \leq 500$ m.

- FINO1



- FINO3

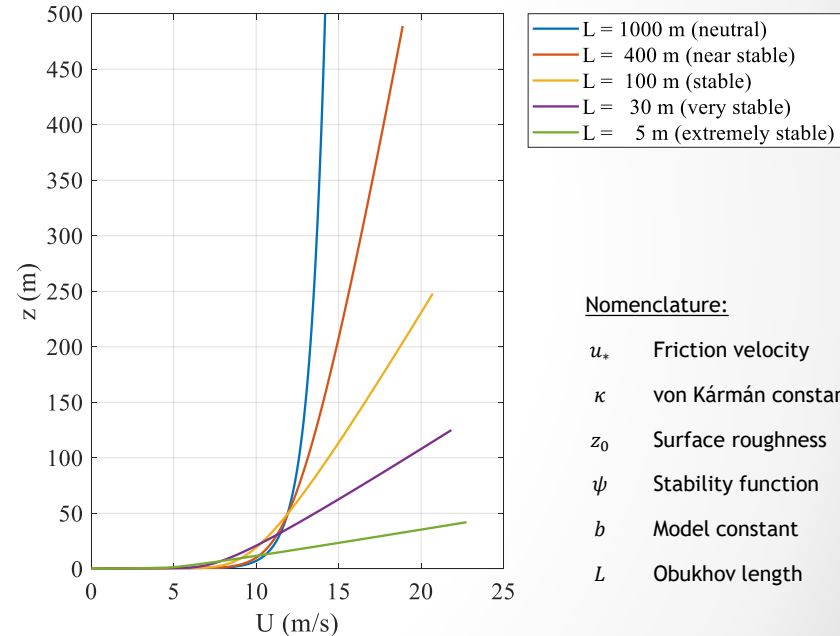


Analytical Wind Profile Models

Logarithmic Wind Profile

Surface layer theory with stability correction:

- $U(z) = \frac{u_*}{\kappa} \left[\ln\left(\frac{z}{z_0}\right) + \psi \right]$
- $\psi = 4.7 \frac{z}{L}$ [9]

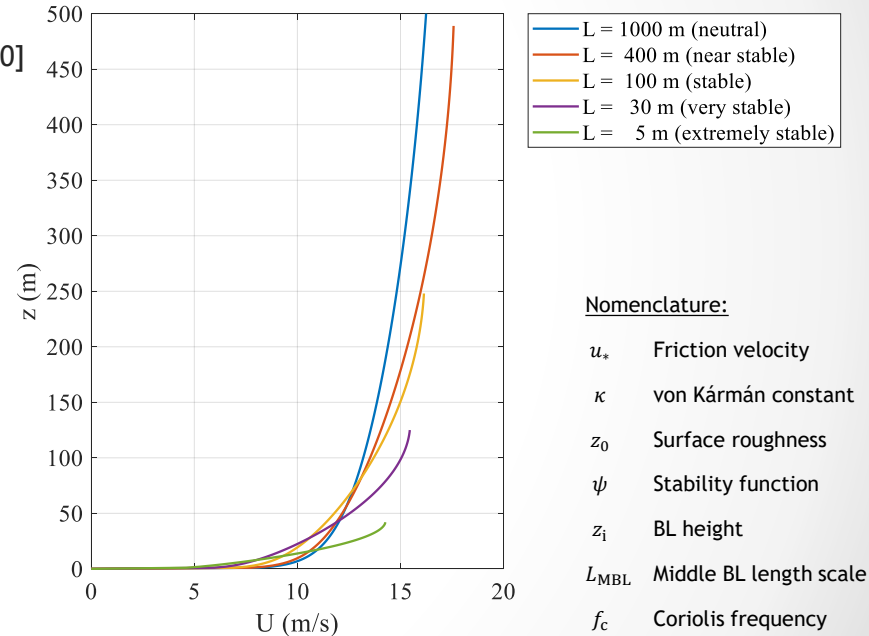


Analytical Wind Profile Models

Gryning Wind Profile

Extension of the logarithmic profile: [10]

- $$U(z) = \frac{u_*}{\kappa} \left[\ln \left(\frac{z}{z_0} \right) - \psi \left(1 - \frac{z}{2 z_i} \right) + \frac{z}{L_{MBL}} - \frac{z}{z_i} \left(\frac{z}{2 L_{MBL}} \right) \right]$$
- $$\frac{u_*}{f_c L_{MBL}} = \left[-2 \ln \left(\frac{u_*}{f_c z_0} \right) + 55 \right] e^{\left[-\frac{u_*^2 / (f_c L)^2}{400} \right]}$$



[10] Gryning, Sven-Erik, Batchvarova, Ekaterina, Brümmner, Burghard, Jørgensen, Hans and Larsen, Søren. "On the extension of the wind profile over homogeneous terrain beyond the surface boundary layer." Boundary-layer meteorology. Vol. 124 (2007): pp. 251-268. DOI 10.1007/s10546-007-9166-9.

Narasimhan Stable ABL Model

Coupling of surface and Ekman layer flow: [11]

Model inputs: L, z_0, f_c, N_∞, G

Streamwise wind velocity:

- $U(\hat{\xi} \leq \hat{\xi}_m) = u_* \left[\frac{1}{\kappa} \ln \left(\frac{\hat{\xi}}{\hat{\xi}_0} \right) + (5\mu + 0.3\mu_N)(\hat{\xi} - \hat{\xi}_0) \right]$
- $U(\hat{\xi} \geq \hat{\xi}_m) = u_* \left[-g'(\hat{\xi}) \left(1 - \frac{\hat{\xi}}{\hat{\xi}_i} \right)^{3/2} + g(\hat{\xi}) \frac{3}{2\hat{\xi}_i} \sqrt{1 - \frac{\hat{\xi}}{\hat{\xi}_i}} \right] + U_g$

Lateral wind velocity:

- $V(\hat{\xi}) = u_* \left[\frac{g(\hat{\xi})g'(\hat{\xi})}{\sqrt{1-g(\hat{\xi})^2}} \left(1 - \frac{\hat{\xi}}{\hat{\xi}_i} \right)^{3/2} + \frac{3}{2\hat{\xi}_i} \sqrt{1-g(\hat{\xi})^2} \left(1 - \frac{\hat{\xi}}{\hat{\xi}_i} \right)^{1/2} \right] + V_g$

- $\hat{\xi} = z f_c / u_*$
- $\hat{\xi}_0 = z_0 f_c / u_*$
- $\hat{\xi}_i = z_i f_c / u_*$
- $\hat{\xi}_m = z_m f_c / u_* = 0.2\hat{\xi}_i$
- $\mu = u_* / (\kappa f_c L)$
- $\mu_N = N_\infty / f_c$
- $g(\hat{\xi}) = c_g \left[1 - e^{-\hat{\xi}/(\Gamma \hat{\xi}_i)} \right]$
- $g'(\hat{\xi}) = \frac{c_g}{\Gamma \hat{\xi}_i} e^{-\hat{\xi}/(\Gamma \hat{\xi}_i)}$
- $c_g = 1.43$
- $\Gamma = 0.83$

Analytical Wind Profile Models

Narasimhan Stable ABL Model

Geostrophic drag law:

- $\frac{\kappa U_g}{u_*} = \ln\left(\frac{u_*}{f_c z_0}\right) - A$
- $\frac{\kappa V_g}{u_*} = -B$
- $G = \sqrt{U_g^2 + V_g^2}$

Derived constants:

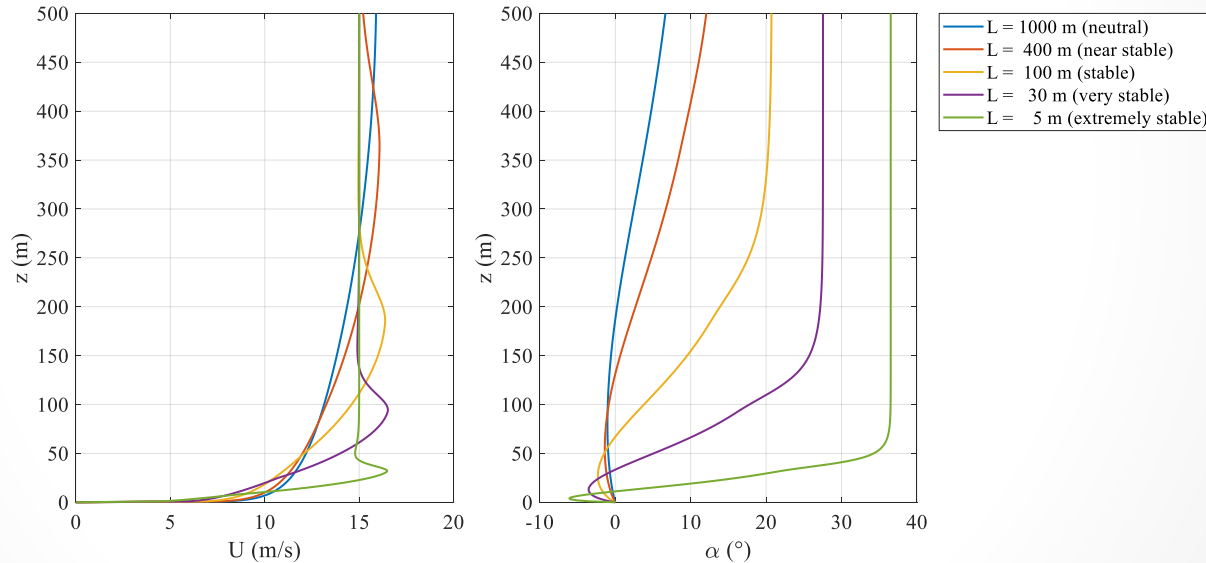
- $A = -\ln \hat{\xi}_m - \kappa \left[(5\mu + 0.3\mu_N)(\hat{\xi}_m - \hat{\xi}_0) + g'(\hat{\xi}_m)(1 - c_m)^{\frac{3}{2}} - g(\hat{\xi}_m) \left(\frac{3}{2}\hat{\xi}_i\right) \sqrt{1 - c_m} \right]$
- $B = \frac{3\kappa}{2\hat{\xi}_i}$
- $c_m = z_m/z_i = 0.2$
- $C_{TN} = 0.5$
- $C_{CN} = 1.6$
- $C_{NS} = 0.78$

Boundary layer height model:

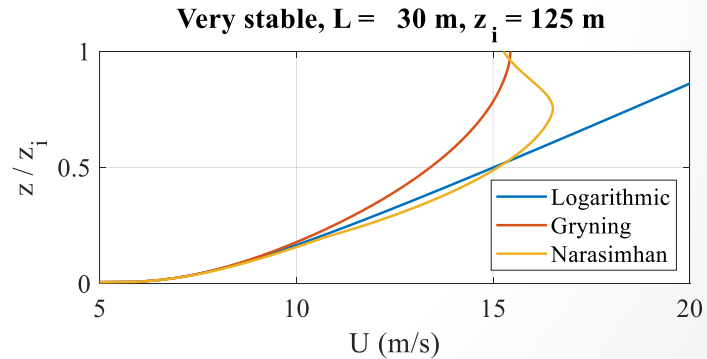
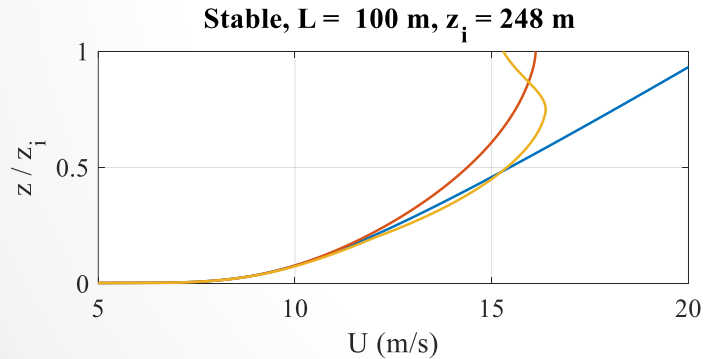
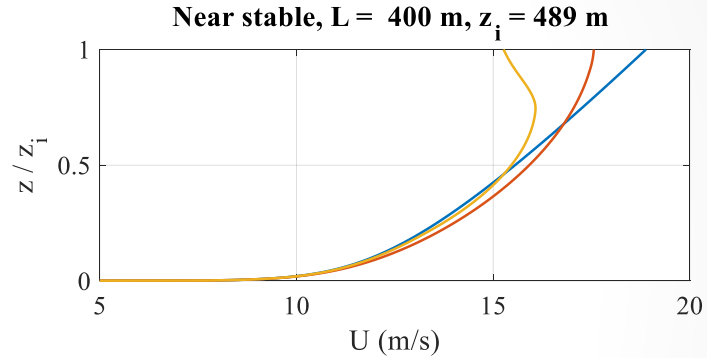
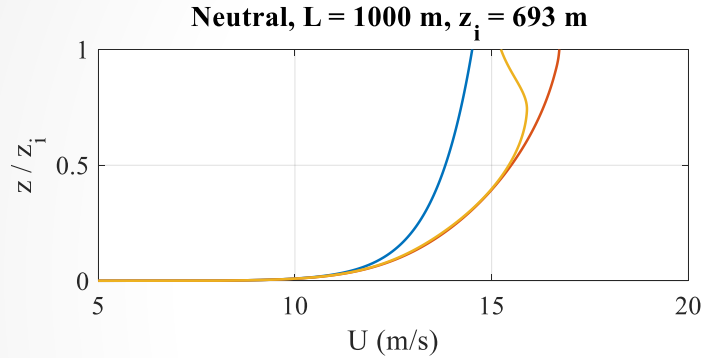
- $\hat{\xi}_i = (C_{TN}^{-2} + C_{CN}^{-2} \mu_N + C_{NS}^{-2} \mu)^{-1/2}$

Narasimhan Stable ABL Model

Resulting wind velocity and direction profiles:



Model Comparison for Different Stability Conditions



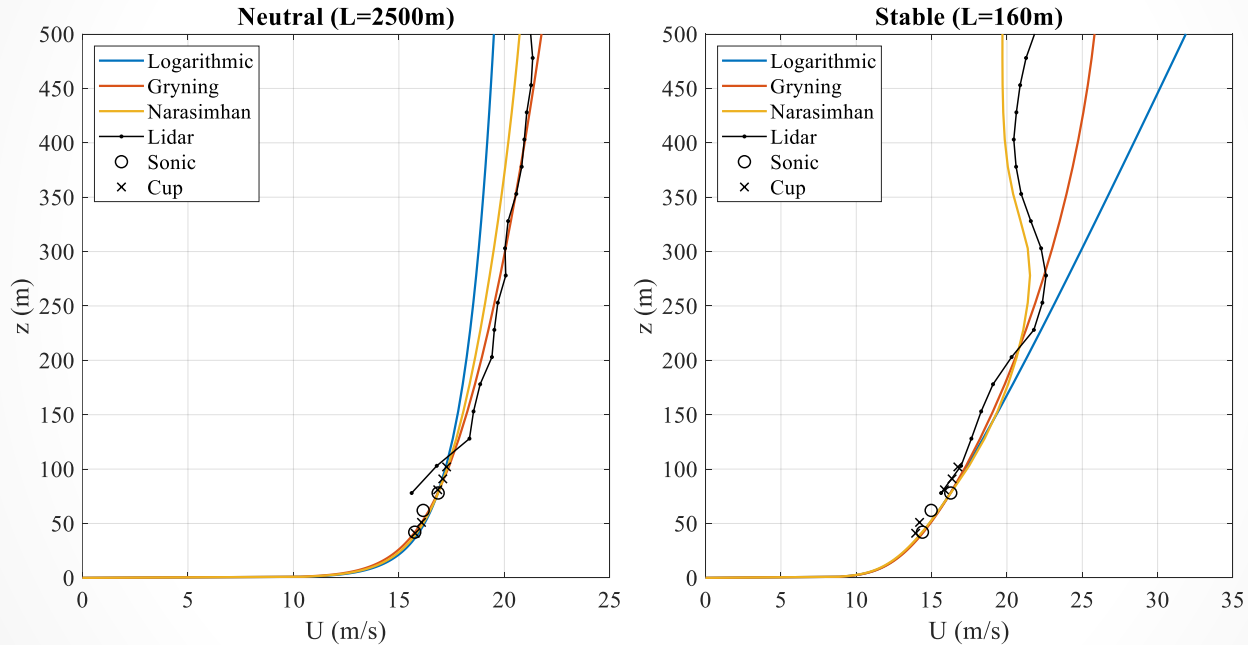
Analytical Wind Profile Models

Model Parametrization

Parameter		Logarithmic	Gryning	Narasimhan	Source
Geostrophic wind velocity	G				Fitted to sonic anemometer wind speed at $z = 81 \text{ m} 101 \text{ m}$
Friction velocity	u_*				Fitted to sonic anemometer wind speed at $z = 81 \text{ m} 101 \text{ m}$
Obukhov length	L				From ERA5 hindcast data
Surface roughness	z_0				From Charnock's relation using $C = 0.018$
Coriolis frequency	f_c				From FINO1 FINO3 latitude
Boundary layer height	z_i				From ERA5 hindcast data

Wind Profile Comparison

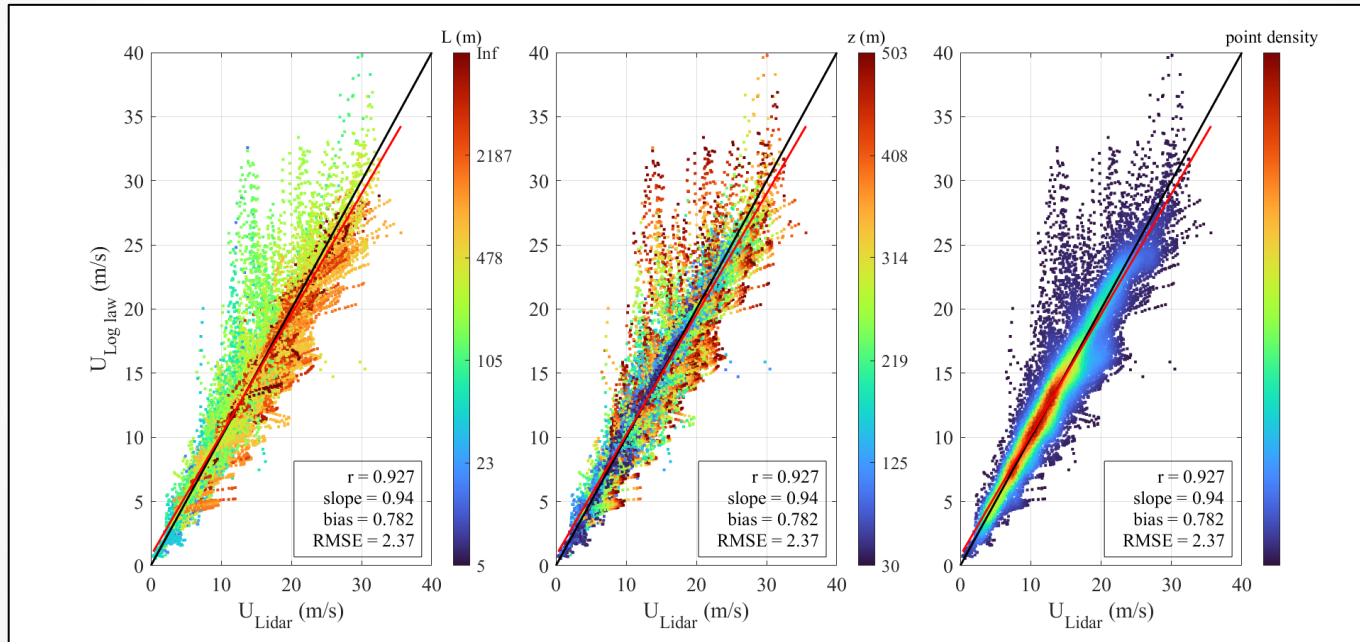
Exemplary 10-minute Profiles Recorded at FIN01



Wind Profile Comparison

Logarithmic Velocity Profile vs. Observations

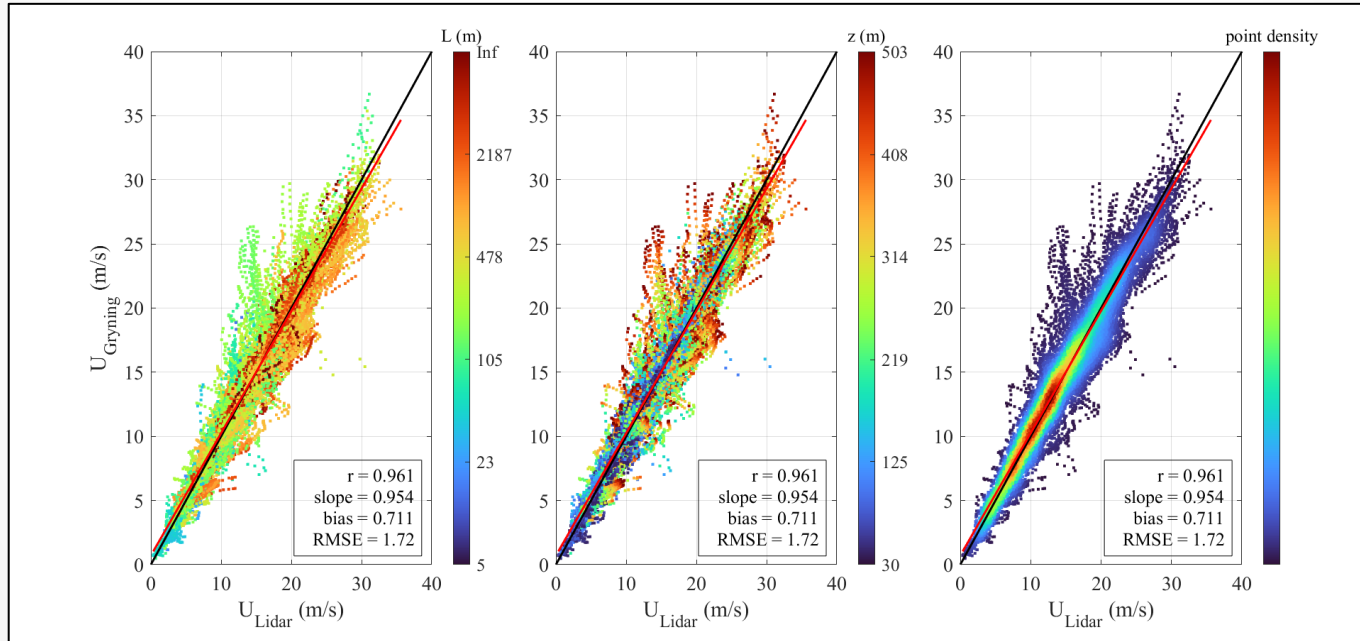
Data from FIN01 for $L \geq 0$ and $z \leq \min(z_i, 500 \text{ m})$.



Wind Profile Comparison

Gryning Velocity Profile vs. Observations

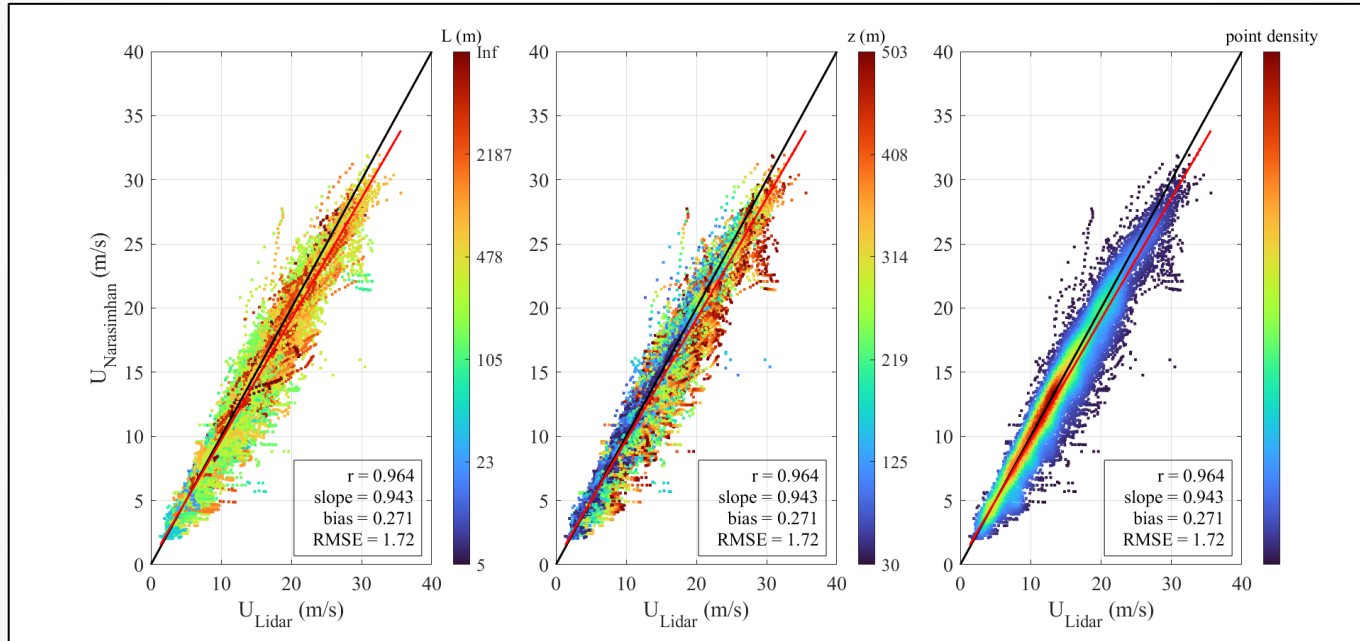
Data from FIN01 for $L \geq 0$ and $z \leq \min(z_i, 500 \text{ m})$.



Wind Profile Comparison

Narasimhan Velocity Profile vs. Observations

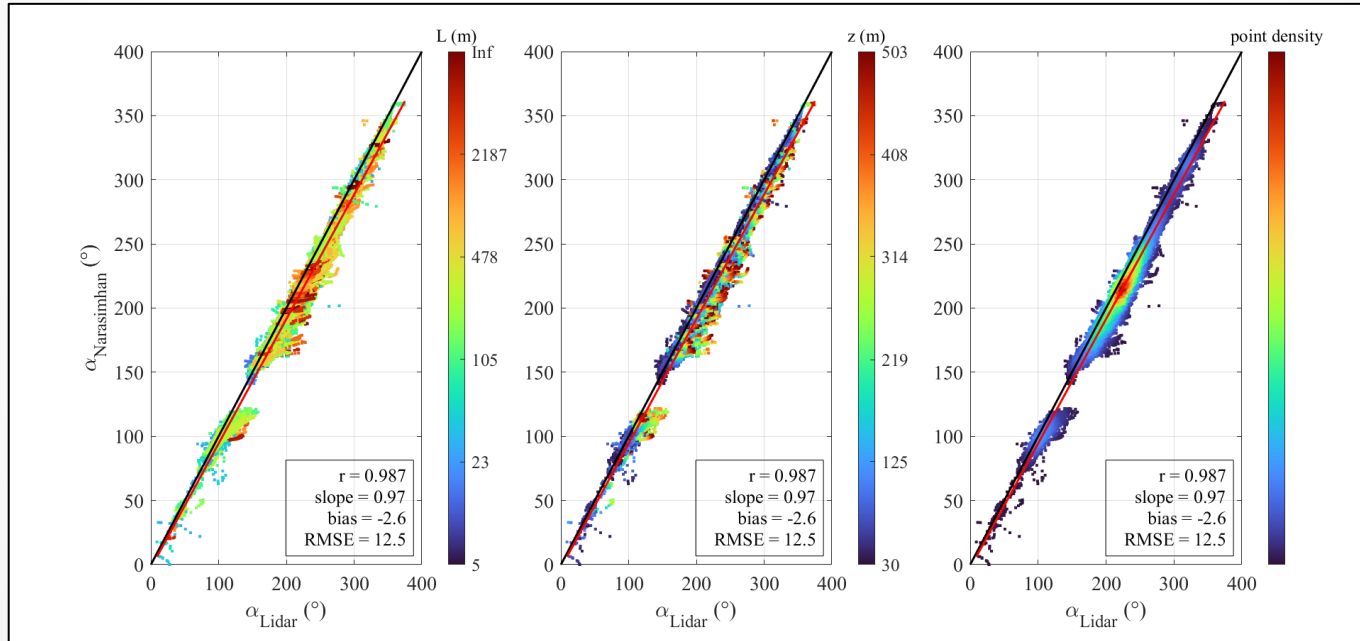
Data from FIN01 for $L \geq 0$ and $z \leq \min(z_i, 500 \text{ m})$.



Wind Profile Comparison

Narasimhan Direction Profile vs. Observations

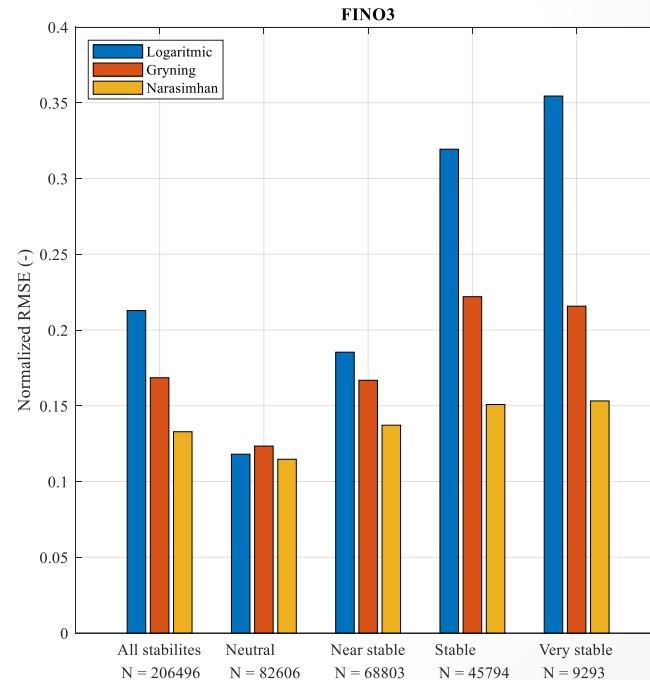
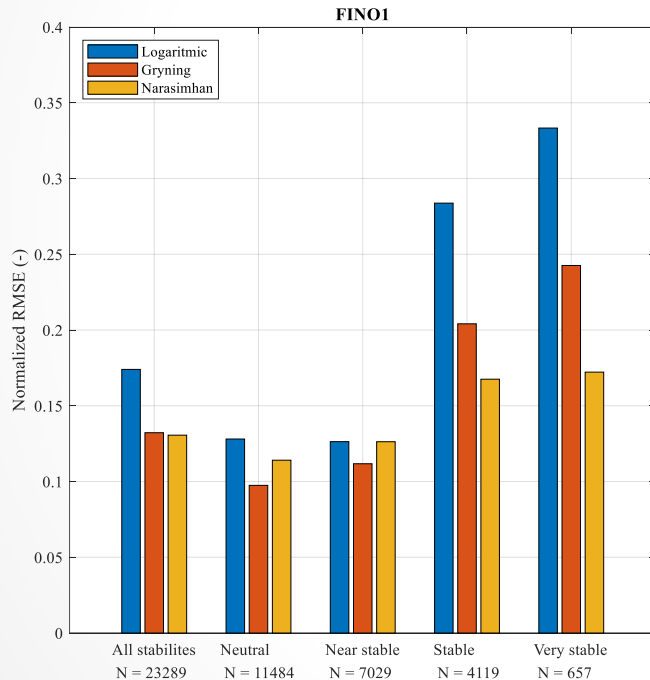
Data from FIN01 for $L \geq 0$ and $z \leq \min(z_i, 500 \text{ m})$.



Wind Profile Comparison

Deviations Between Modelled and Observed Profiles

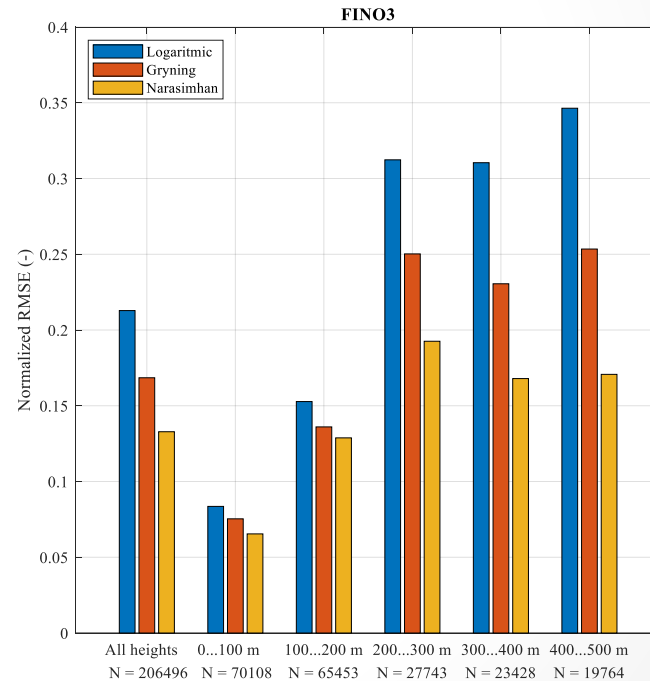
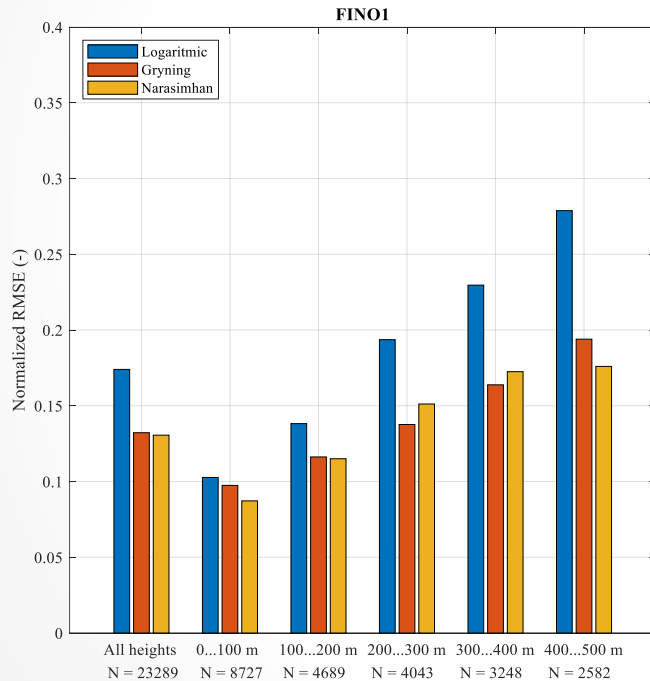
Normalized RMSE across wind profile models and atmospheric stability.



Wind Profile Comparison

Deviations Between Modelled and Observed Profiles

Normalized RMSE across wind profile models and height.

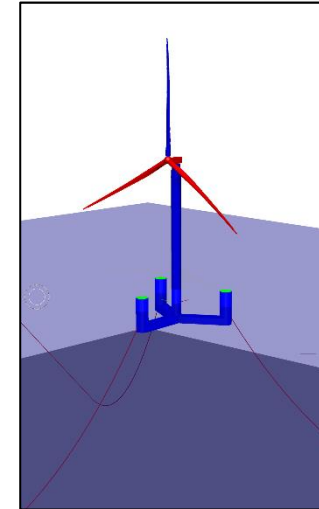
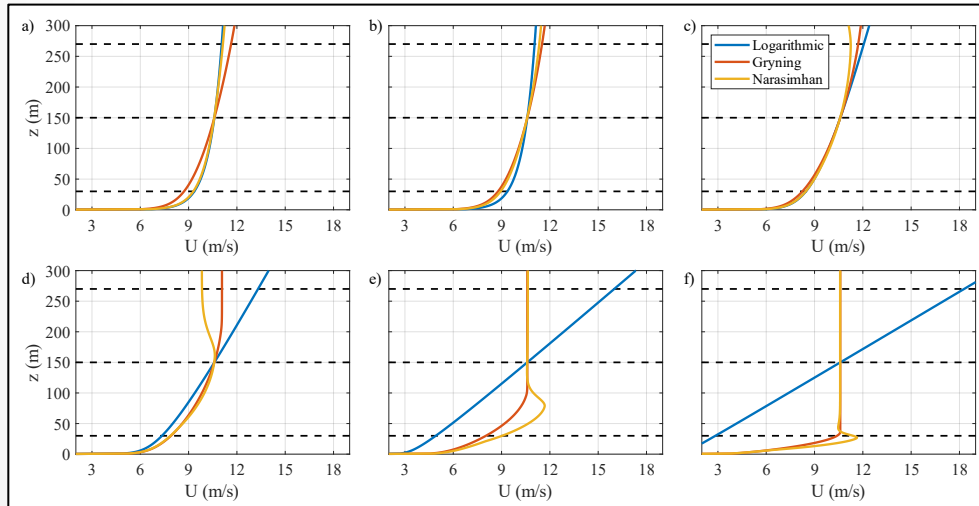



Conclusion

- Tall lidar profiles observed at FINO1 and FINO3...
 - ... supplemented with mast data.
 - ... classified using ERA5 Obukhov length estimate.
- 3 analytical profile models parameterized and compared with observations.
- Neutral to near-stable conditions:
 - All models perform similarly well.
 - Logarithmic profile shows slightly larger deviations.
- Stable to very stable conditions:
 - Narasimhan profile shows lowest deviations.
 - Logarithmic profile shows largest deviations.
- Deviations further increase with height for all models.

Outlook

Subsequent study: L Vogt, J B Jakobsen, J B de Vaal: “Sensitivity of Floating Wind Turbine Response to Stable Boundary Layer Wind Profiles”





Thank you for your attention!